

# Memory-driven mixed low precision quantization for enabling deep inference networks on microcontrollers

**Manuele Rusci\***, Alessandro Capotondi, Luca Benini

[\\*manuele.rusci@unibo.it](mailto:manuele.rusci@unibo.it)

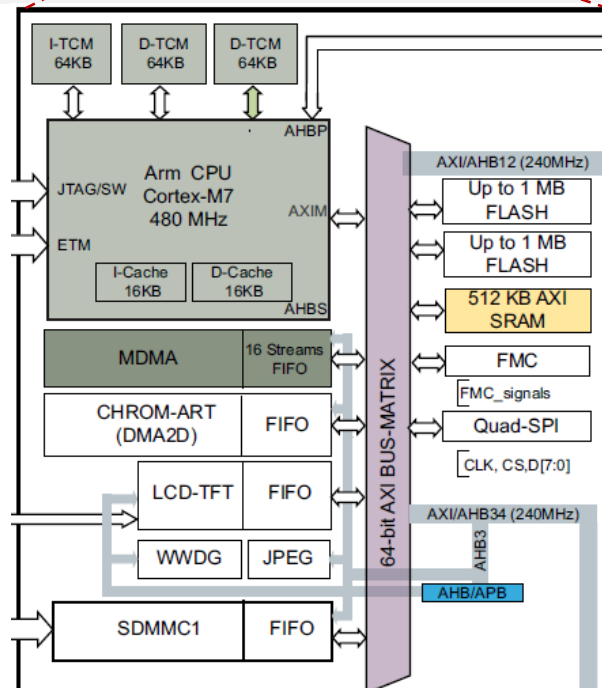
*Energy-Efficient Embedded Systems Laboratory*

Dipartimento di Ingegneria dell'Energia Elettrica e dell'Informazione  
"Guglielmo Marconi" – DEI – **Università di Bologna**

# Microcontrollers for smart sensors



# Microcontrollers for smart sensors



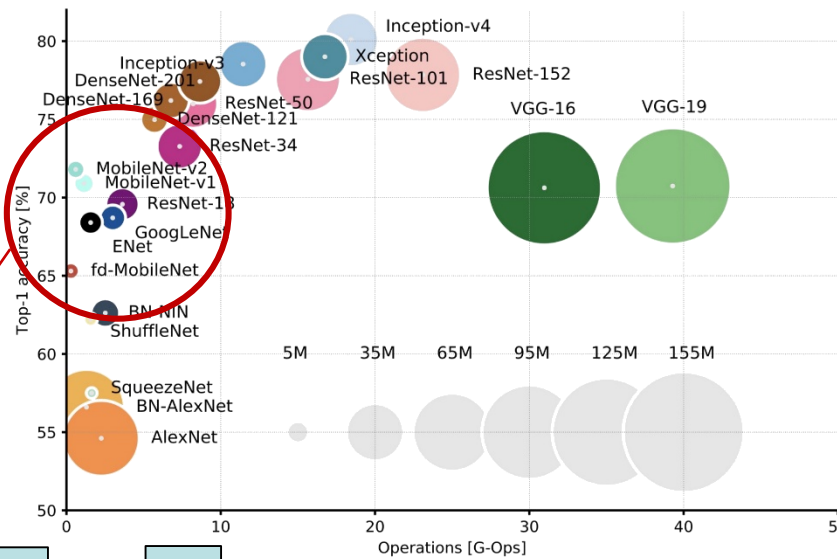
Source: STM32H7 datasheet

- ❑ Low-power (<10-100mW) & low-cost
  - ❑ Smart device are battery- operated
- ❑ Highly-flexible (SW programmable)
- ❑ But **limited resources(!)**
  - ❑ few MB of memories
  - ❑ single RISC core up to few 100s MHz (STM32H7: 400MHz) with DSP SIMD instructions and optional FPU
- ❑ Currently, tiny visual DL tasks on MCUs (visual wake words, CIFAR10)

**Challenge:** Run 'complex' and 'big' (Imagenet-size) DL inference on MCU ?

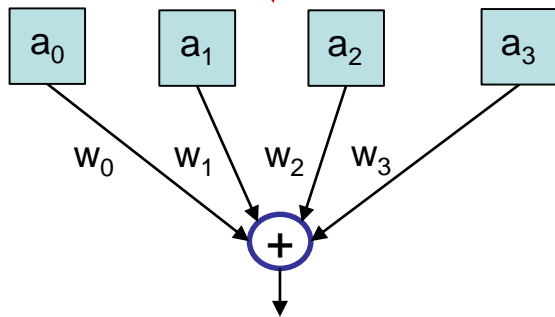
# Deep Learning for microcontrollers

“Efficient” topologies: Accuracy **vs MAC vs Memory**



Source: <https://towardsdatascience.com/neural-network-architectures-156e5bad51ba>

But  
**quantization**  
is also  
essential...



Reducing bit  
precision

<b>FP32</b>	: 4 instr	+ 32 bytes
<b>INT16</b>	: 2 instr	+ 16 bytes
<b>INT8</b>	: 1 instr	+ 8 bytes

(if ISA MAC SIMD available)

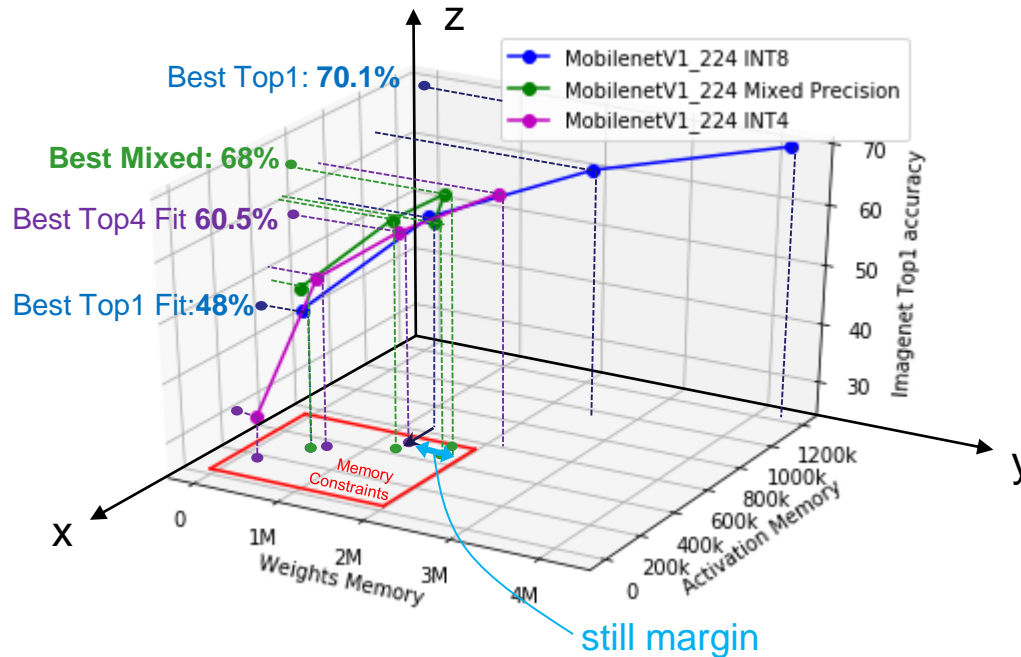
Memory  
Accuracy  
Compute

**Issue1:** Integer-only model needed for deployment on low-power MCUs

**Issue2:** 8-16 bit are **not** sufficient to bring ‘complex’ models on MCUs (memory!!)

# Memory-Driven Mixed-Precision Quantization

Using less than 8 bits...



apply minimum tensor-wise quantization  $\leq 8\text{bit}$  to fit the **memory constraints** with very-low accuracy drop

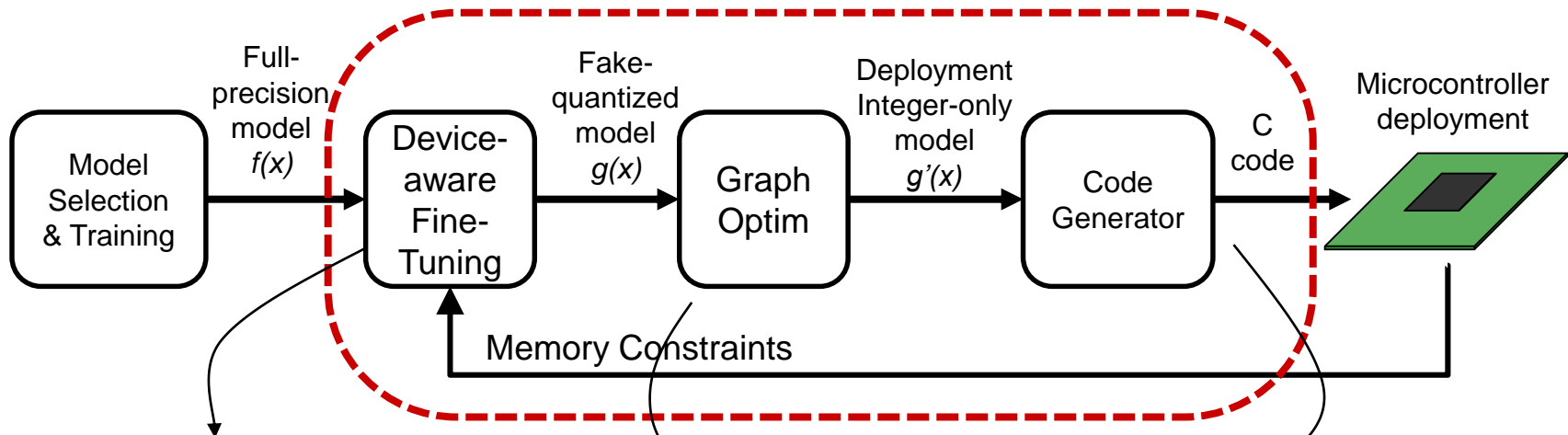
## ➤ Challenges:

- How to define the quantization policy
- Combine quantization flow this with integer only transformation

# End-to-end Flow & Contributions

**Goal:** Define a design flow to bring Imagenet-size models into an MCU device while paying a low accuracy drop.

## DNN Development Flow for microcontrollers



### Device-aware Fine-Tuning

We define a rule-based methodology to determine the **mixed-precision quantization policy** driven by a memory objective function.

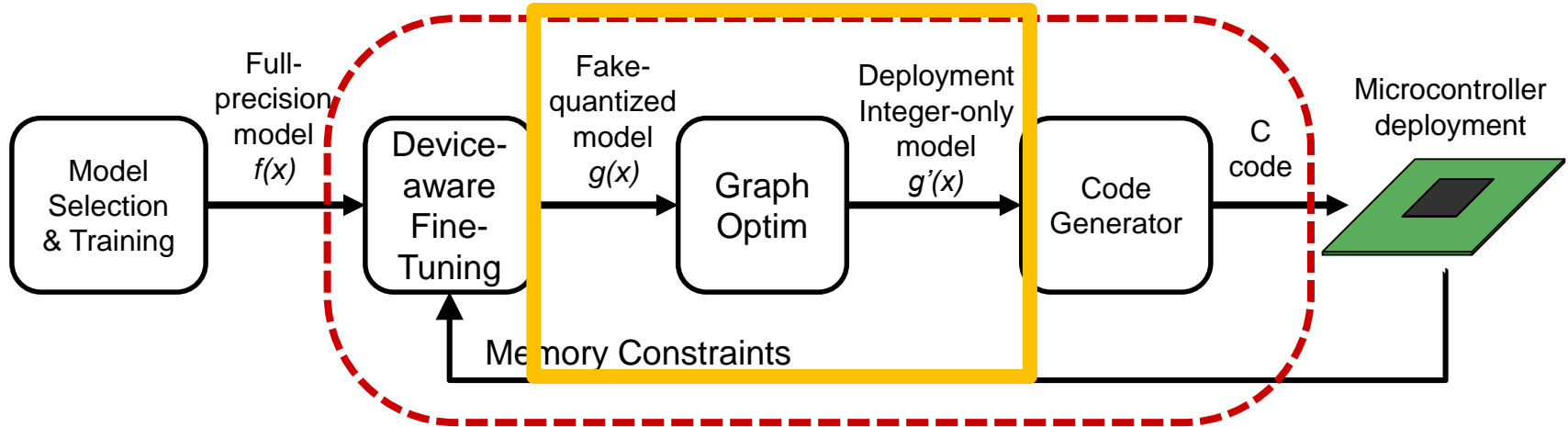
### Graph Optimization

We introduce the **Integer Channel-Normalization** (ICN) activation layer to generate an **integer-only deployment** graph when applying **uniform sub-byte quantization**.

### Deployment on MCU

A **latency-accuracy tradeoff** on iso-memory mixed-precision networks belonging to the **Imagenet MobilenetV1** family when running on a **STM32H7** MCU.

## DNN Development Flow for microcontrollers



Graph Optimization

**INTEGER-ONLY  
W/ SUB-BYTE  
QUANTIZATION**



# State of the Art

- ❑ Inference with Integer-only arithmetic (Jacob, 2018)
  - ❑ Affine transformation between real value and (uniform) quantized parameters
  - ❑ Quantization-aware retraining
  - ❑ Folding of batch norm into conv weights + rounding of per-layer scaling parameters

$$\begin{array}{l} \text{real value} \\ \text{tensor or sub-} \\ \text{tensor} \end{array} \rightarrow t = S_t \times \begin{array}{l} \text{quantized tensor (INT-Q)} \\ \swarrow \\ (T_q - Z_t) \end{array}$$

- 😊 Almost lossless with 8 bit on Image classification and detection problems. Used by TF Lite.
- ☹️ 4 bit MobilnetV1: Training collapse when folding batch norm into convolution weights
- ☹️ Does not support Per-Channel (PC) weight quantization

Integer-Only MobilenetV1\_224\_1.0

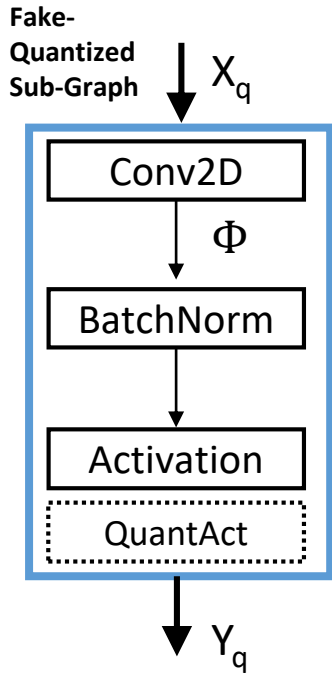
Quantization Method	Top1	Weights (MB)
Full-Precision	70.9	16.8
w8a8	70.1	4.06
w4a4	0.1	2.05

(Jacob, 2018) Jacob, Benoit, et al. "Quantization and training of neural networks for efficient integer-arithmetic-only inference." CVPR 2018





# Integer-Channel Normalization (ICN)



$$Y_q = \text{quant}_{act} \left( \frac{\phi - \mu}{\sigma} \cdot \gamma + \beta \right)$$

$$\phi = \sum w \cdot x$$

$\mu, \sigma, \gamma, \beta$  are channel-wise batchnorm parameters

Replacing  $t = S_t \times (T_q - Z_t)$

$S_w$  is scalar if PL, else array  
 $S_i, S_o$  are scalar

$$\Phi = \sum (W_q - Z_w) \cdot (X_q - Z_x)$$

$$Y_q = Z_y + \text{quant}_{act} \left( \frac{S_i S_w}{S_o} \frac{\gamma}{\sigma} \left( \Phi + \left[ \frac{1}{S_i S_w} \left( B - \mu + \frac{\beta \sigma}{\gamma} \right) \right] \right) \right)$$

$$M_0 2^{N_0} (\Phi + B_q)$$

$M_0, N_0, B_q$  are channel-wise integer params

Integer-Only MobilenetV1\_224\_1.0

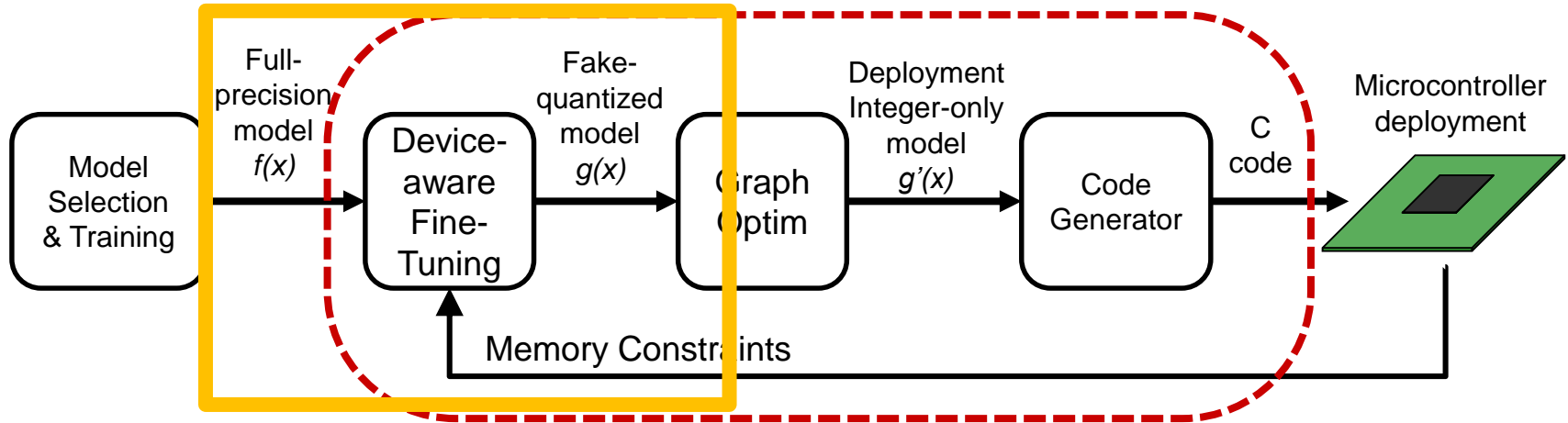
Quantization Method	Top1	Weights (MB)
Full-Precision	70.9	16.8
PL+ICN w4a4	61.75	2.10
PC+ICN w4a4	66.41	2.12

## Integer Channel-Normalization (ICN)

activation function

- holds either for PL or PC quantization of weights

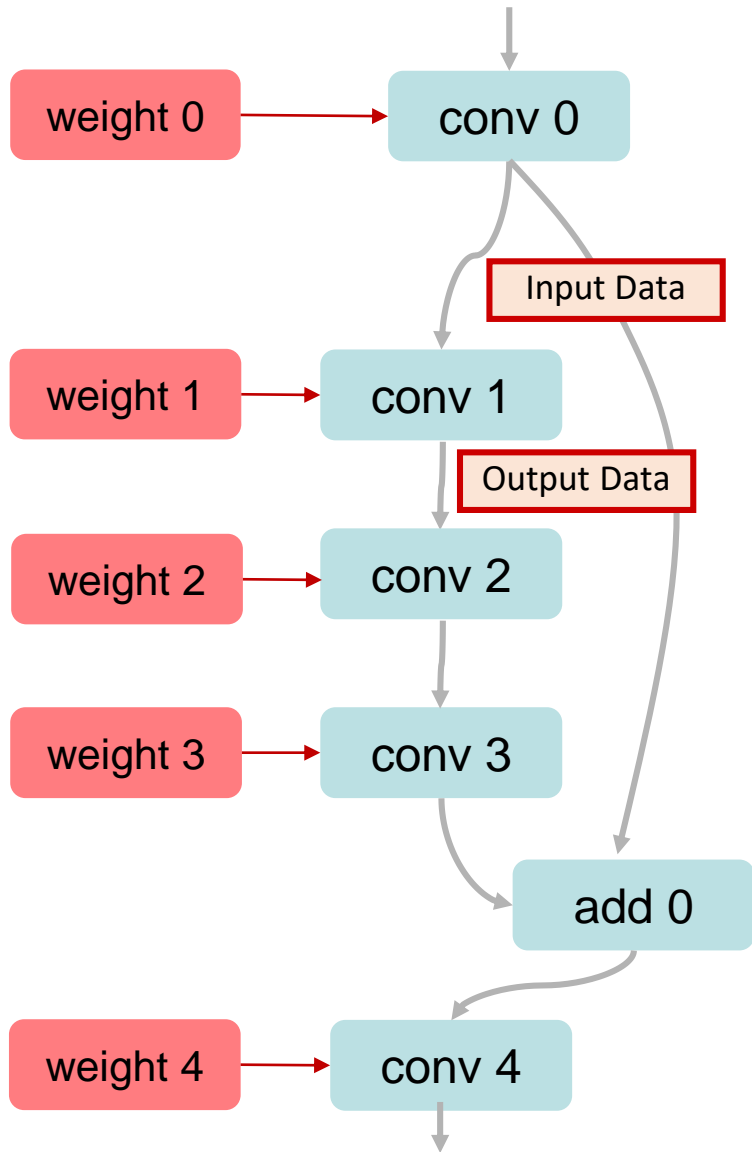
## DNN Development Flow for microcontrollers



Device-aware Fine-Tuning

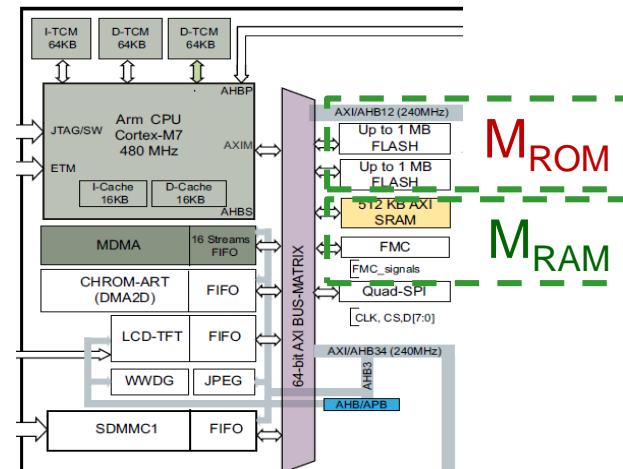
# MIXED-PRECISION QUANTIZATION POLICY

# Deployment of an integer-only graph

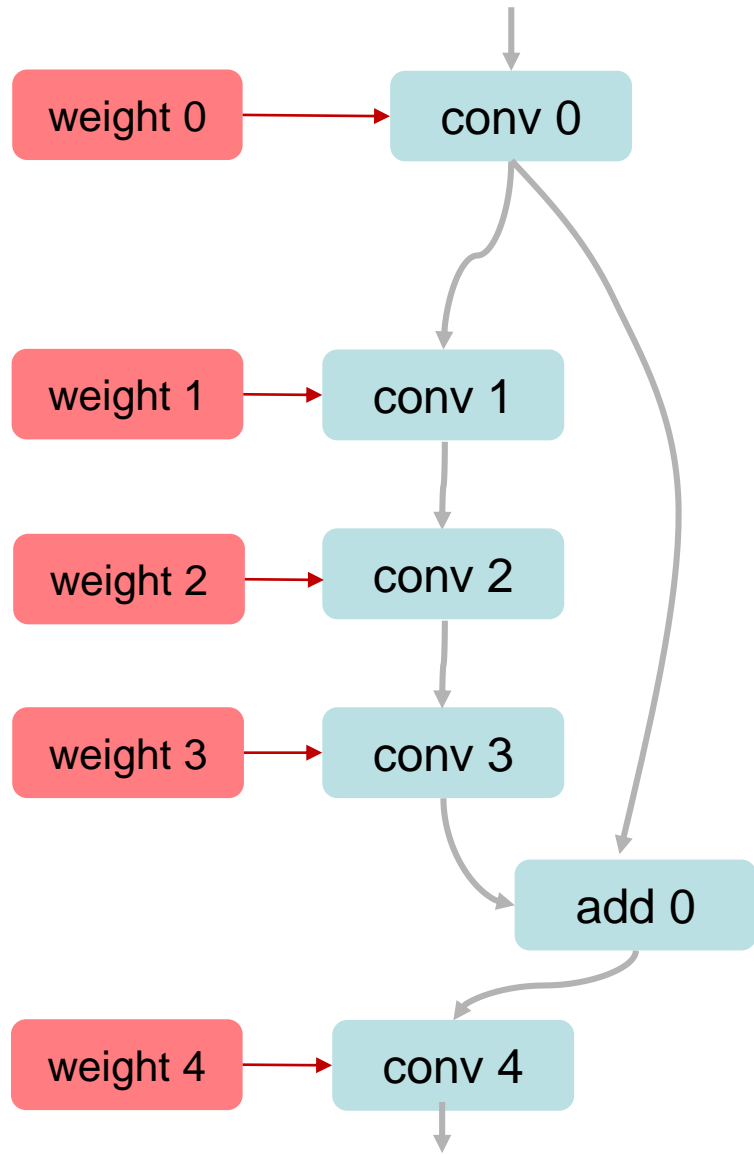


## Problem

Can this graph fit the memory constraints of our MCU device?

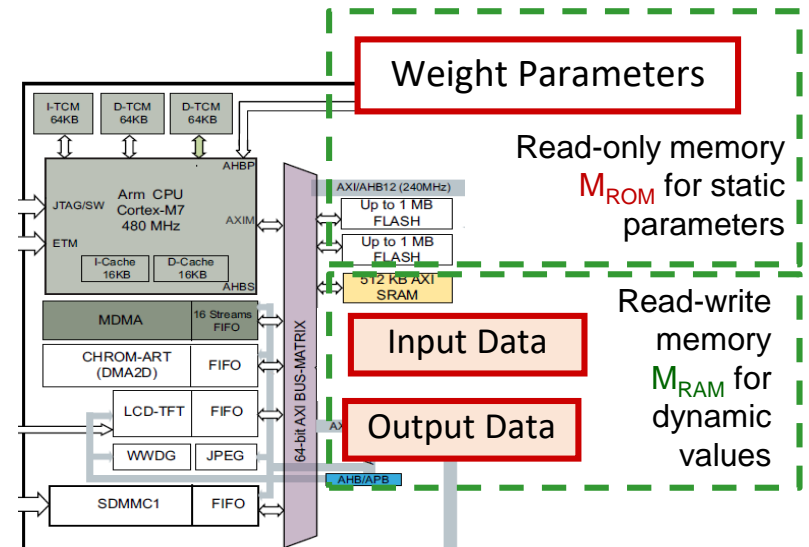


# Deployment of an integer-only graph

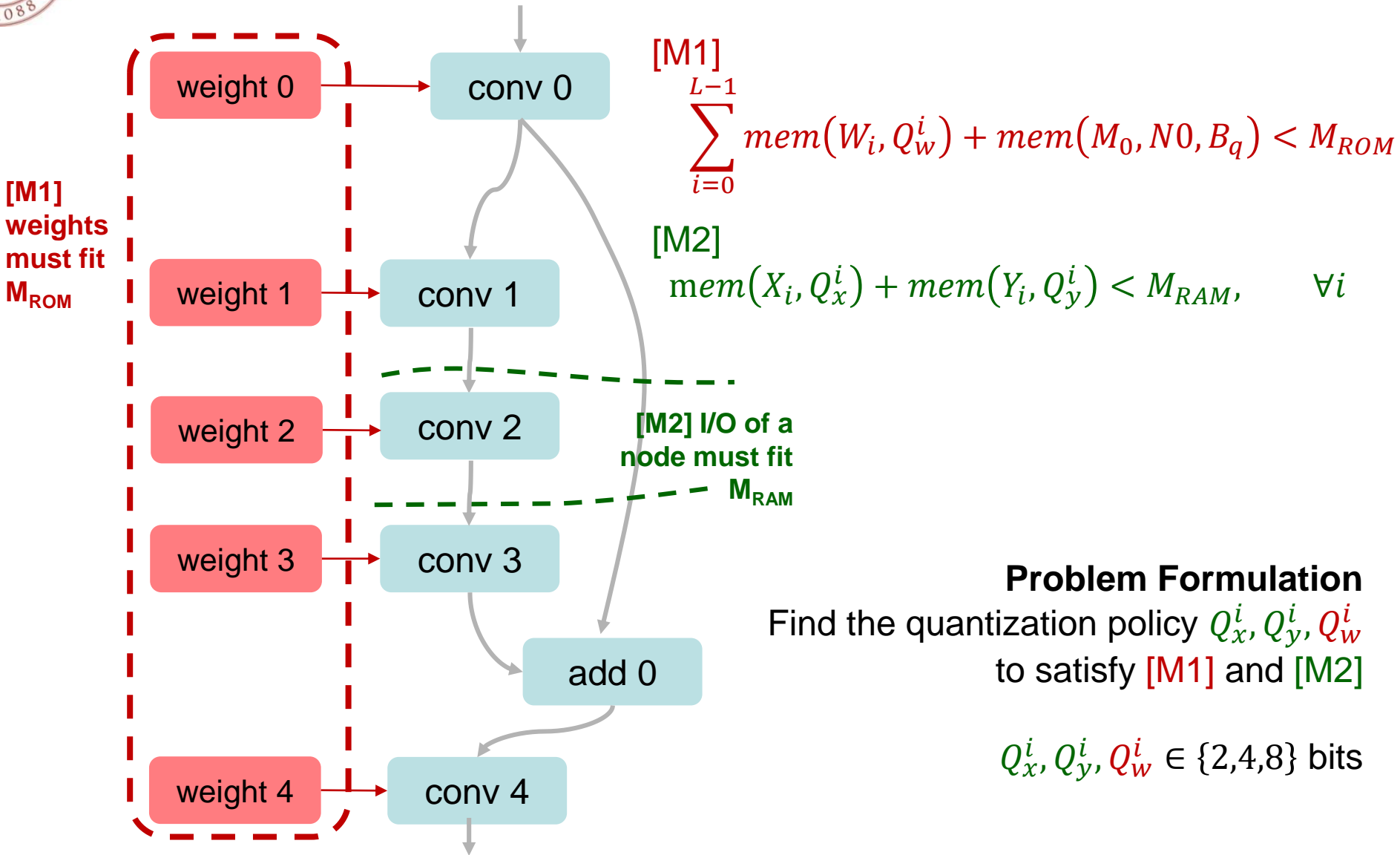


## Problem

Can this graph fit the memory constraints of our MCU device?

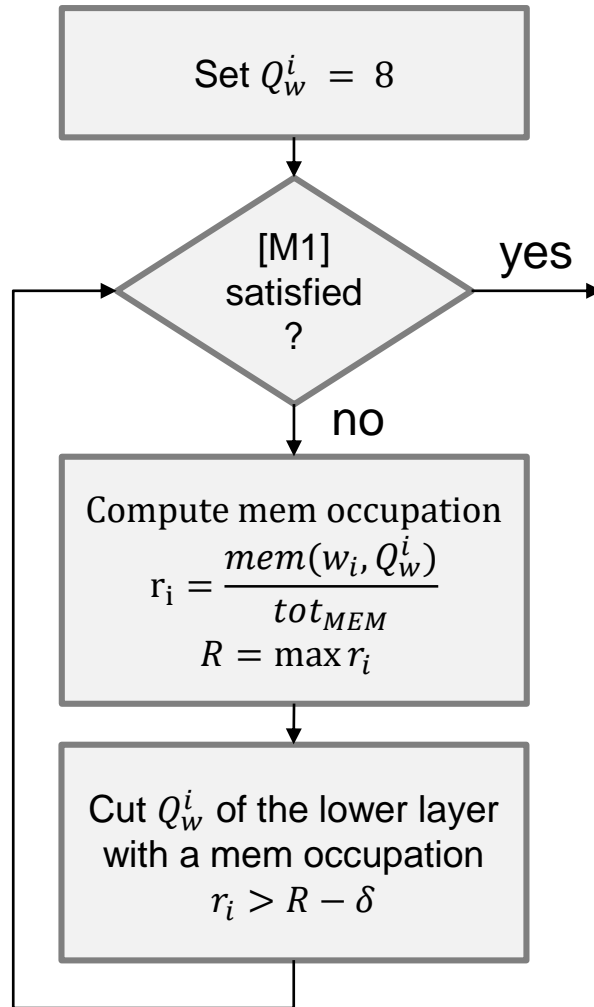


# Deployment of an integer-only graph



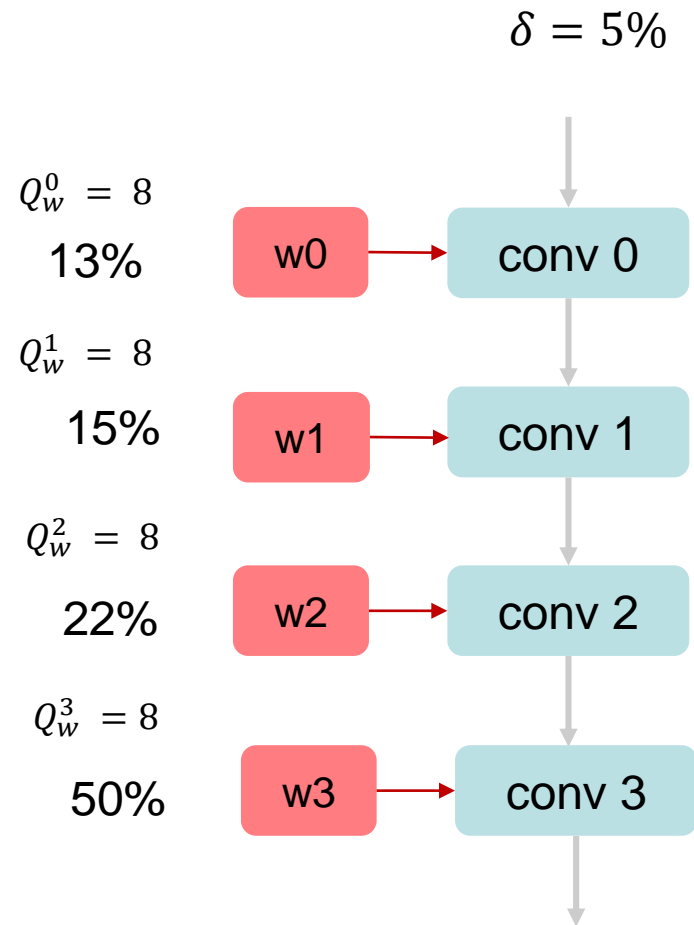
# Rule-Based Mixed-Precision

**Goal**  
Maximize  
memory  
utilization



**Weights**  
**Quantization Policy**

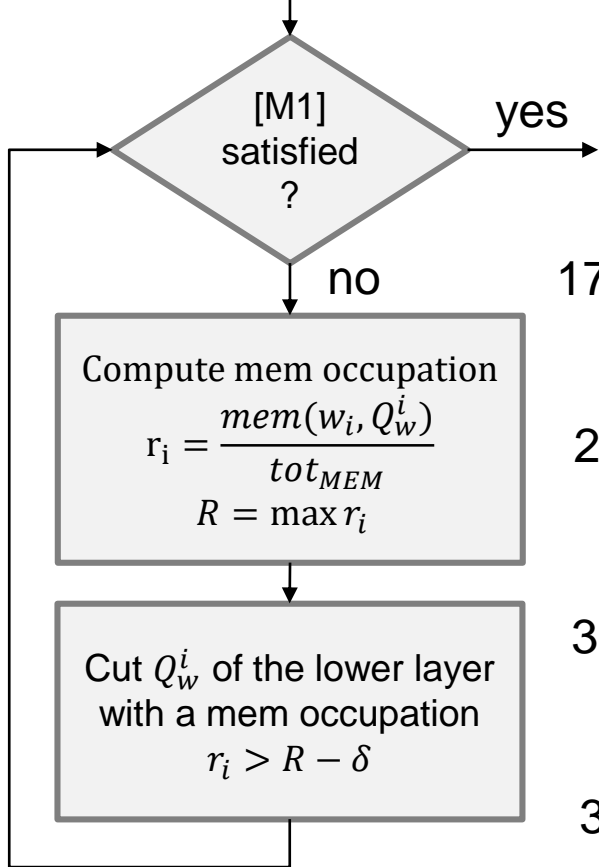
$$[M1] : \text{size}(w_0) + \text{size}(w_1) + \text{size}(w_2) + \text{size}(w_3) < M_{ROM}$$



# Rule-Based Mixed-Precision

**Goal**  
Maximize  
memory  
utilization

Set  $Q_w^i = 8$



$$[M1] : \text{size}(w_0) + \text{size}(w_1) + \text{size}(w_2) + \text{size}(w_3) < M_{ROM}$$

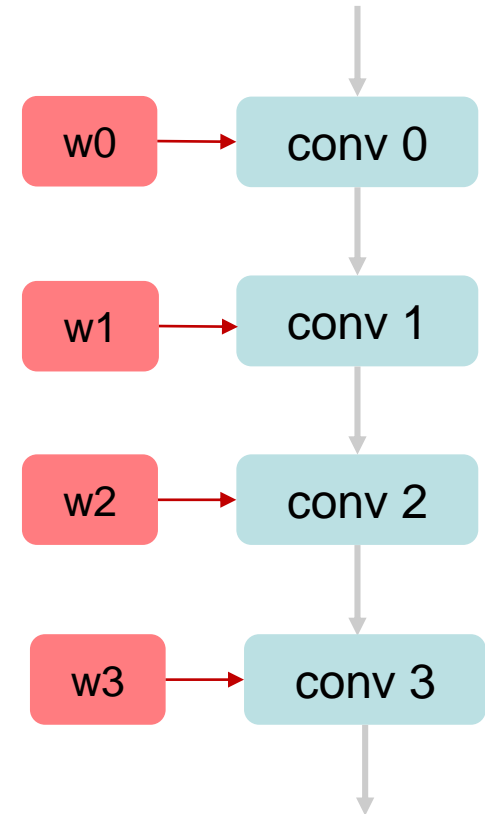
$\delta = 5\%$

$Q_w^0 = 8$   
17% ← 13%

$Q_w^1 = 8$   
20% ← 15%

$Q_w^2 = 8$   
30% ← 22%

$Q_w^3 = 4$   
33% ← 50%



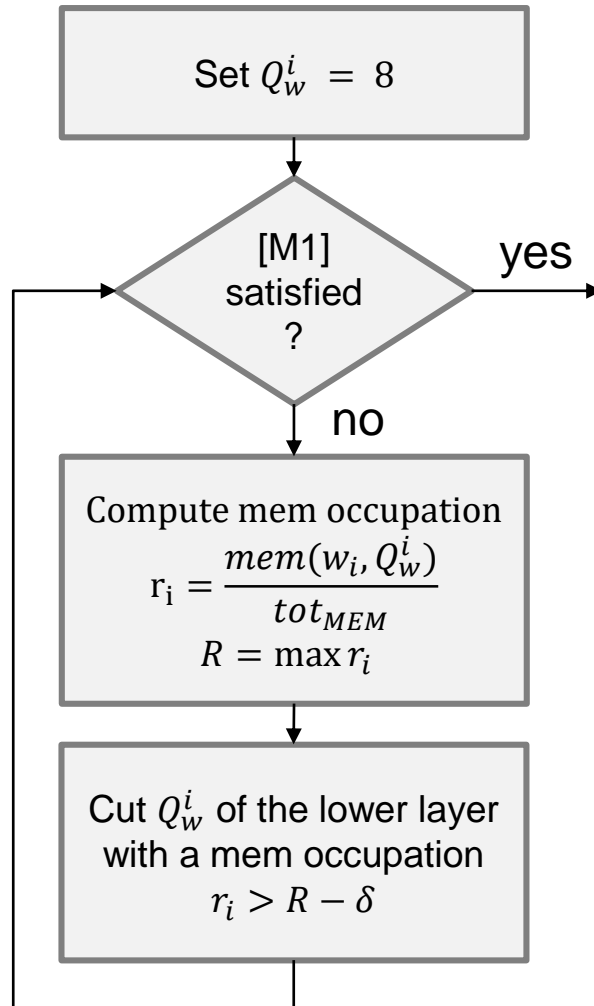
**Weights**  
**Quantization Policy**

Cut layer 3!

Any cut reduces  
the bit precision by  
one step: 8→4,  
4→2

# Rule-Based Mixed-Precision

**Goal**  
Maximize  
memory  
utilization



**Weights**  
**Quantization Policy**

$$[M1] : \text{size}(w_0) + \text{size}(w_1) + \text{size}(w_2) + \text{size}(w_3) < M_{ROM}$$

$\delta = 5\%$

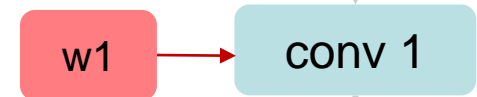
$$Q_w^0 = 8$$

17%



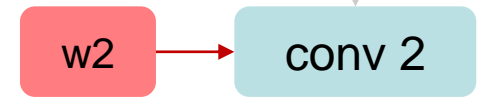
$$Q_w^1 = 8$$

20%



$$Q_w^2 = 4$$

30%



$$Q_w^3 = 4$$

33%



Cut layer 2!

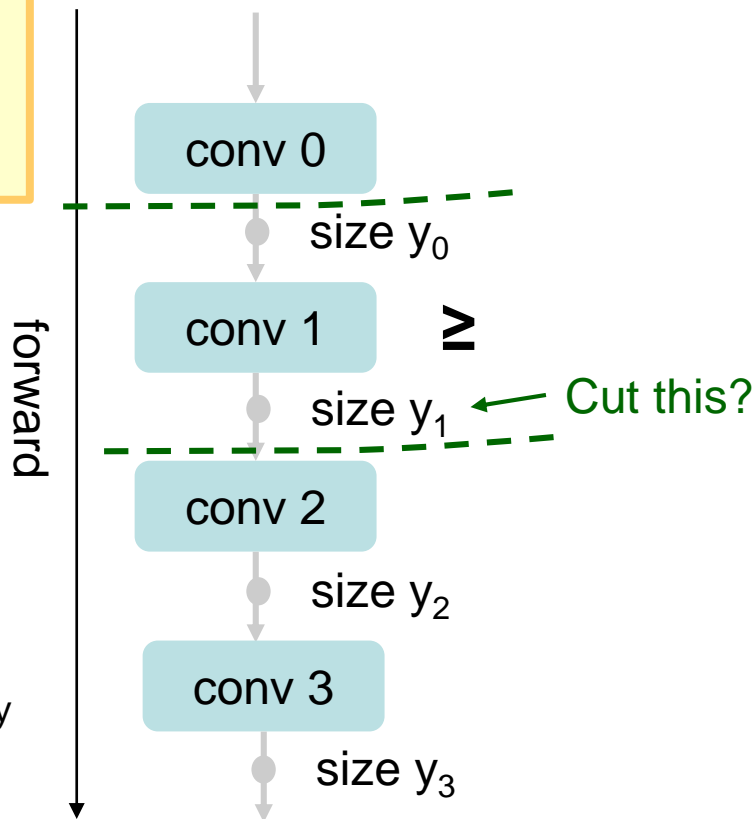
Any cut reduces  
the bit precision by  
one step: 8→4,  
4→2





# Rule-Based Mixed-Precision

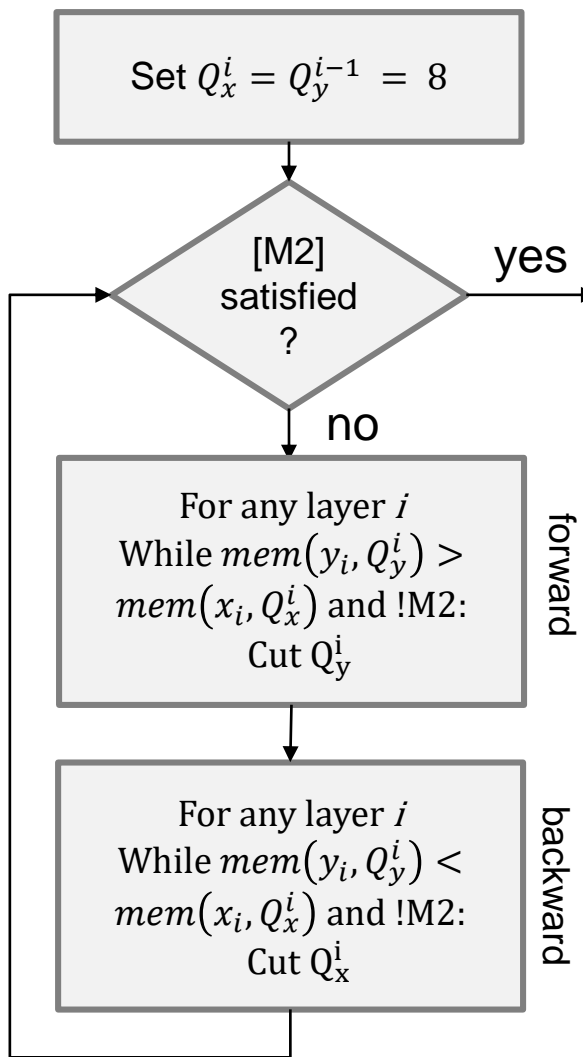
**Goal**  
Maximize  
memory  
utilization



Any cut reduces  
the bit precision by  
one step: 8→4,  
4→2

**[M2]** {

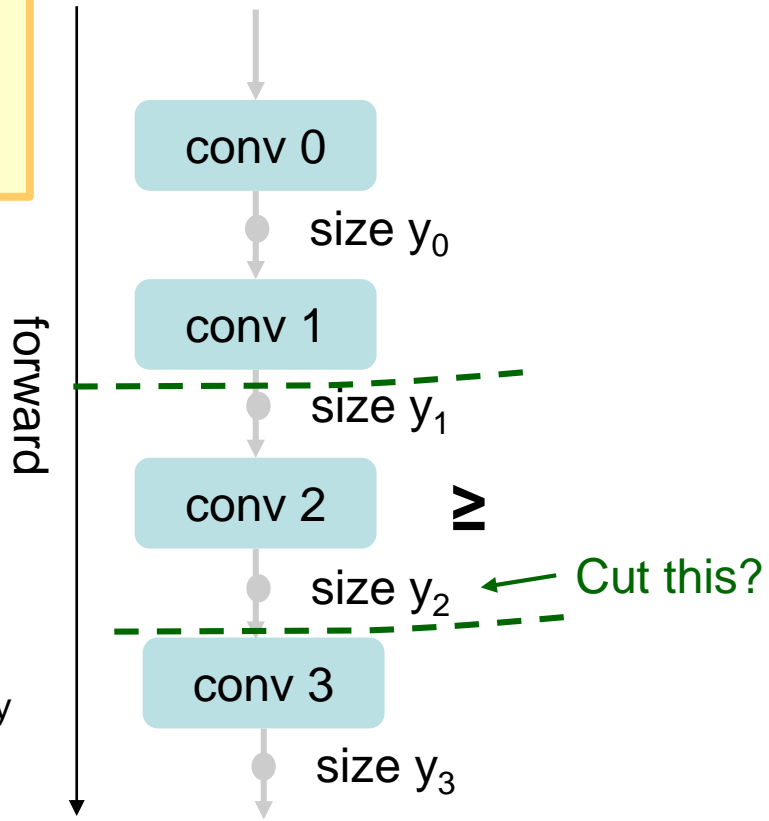
- size  $y_0$  + size  $y_1$  <  $M_{RAM}$
- size  $y_1$  + size  $y_3$  <  $M_{RAM}$
- size  $y_2$  + size  $y_3$  <  $M_{RAM}$



**Activation  
Quantization Policy**

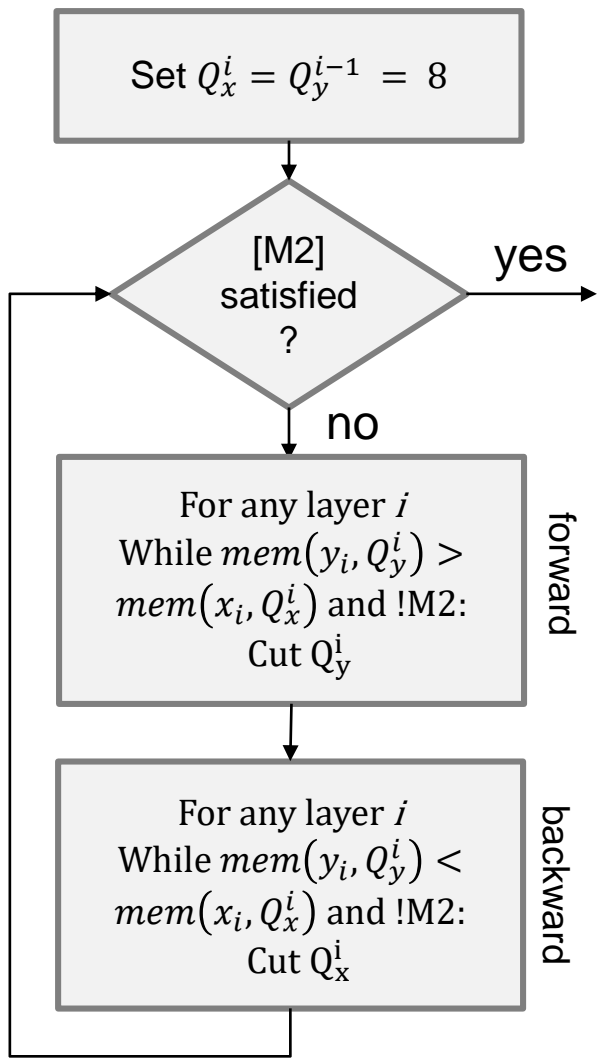
# Rule-Based Mixed-Precision

**Goal**  
Maximize  
memory  
utilization



Any cut reduces  
the bit precision by  
one step: 8→4,  
4→2

**[M2]** {  
size  $y_0$  + size  $y_1$  <  $M_{RAM}$   
size  $y_1$  + size  $y_3$  <  $M_{RAM}$   
size  $y_2$  + size  $y_3$  <  $M_{RAM}$

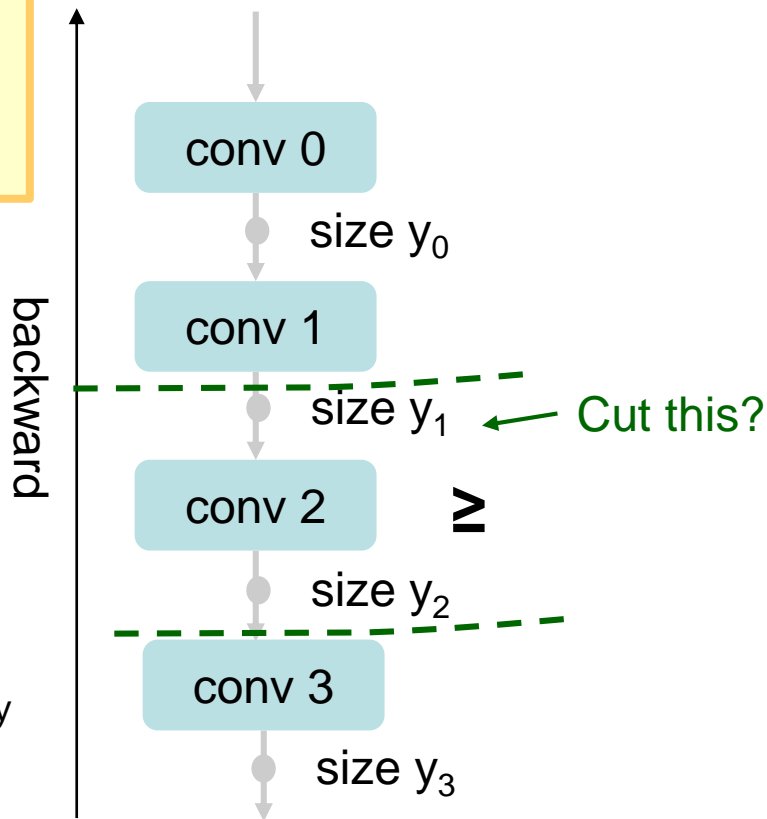


**Activation  
Quantization Policy**



# Rule-Based Mixed-Precision

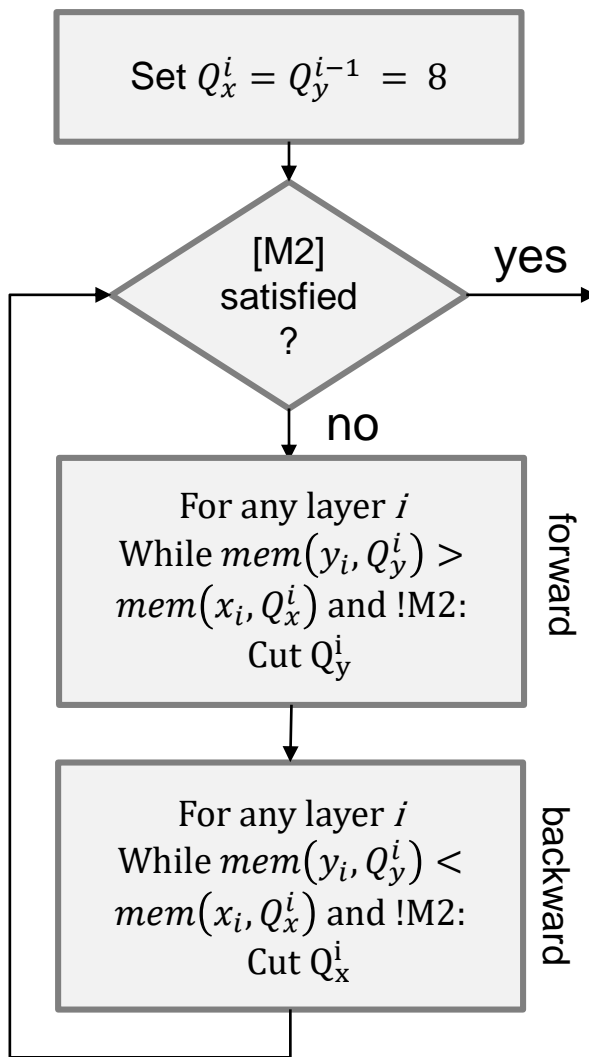
**Goal**  
Maximize  
memory  
utilization



Any cut reduces  
the bit precision by  
one step:  $8 \rightarrow 4$ ,  
 $4 \rightarrow 2$

**[M2]** {

- size  $y_0$  + size  $y_1 < M_{RAM}$
- size  $y_1$  + size  $y_3 < M_{RAM}$
- size  $y_2$  + size  $y_3 < M_{RAM}$



**Activation  
Quantization Policy**



# Experimental Results on MobilenetV1

Iso-memory MobilenetV1 models with 2MB FLASH and 512kB RAM.

Integer-only

Model	Mparams	Full-Prec	Mix-PC	Mix-PL
224_1.0	4.24	<b>70.9</b>	64.3	59.6
192_1.0	4.24	70.0	65.9	61.9
224_0.75	2.59	68.4	<b>68.0</b>	<b>67.0</b>
192_0.75	2.59	67.2	67.2	64.8
224_0.5	1.34	63.3	63.5	63.1
192_0.5	1.34	61.7	62.0	59.5

Quantization-aware Fine-Tuning recipe:

- Init w/ pre-trained params
- 8H on 4 NVIDIA Tesla P100
- ADAM, lr=1e-4 (5e-5 @5ep, 1e-5 at 8 eph)
- Frozen batch norm stats after 1 eph
- Asymmetric quant on weights, either PC (min/max) or PL (PACT)
- Asymmetric activation (PACT)

Open source: <https://github.com/mrusci/training-mixed-precision-quantized-networks>



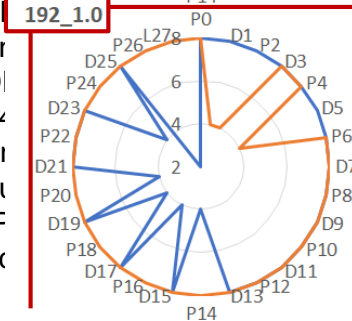
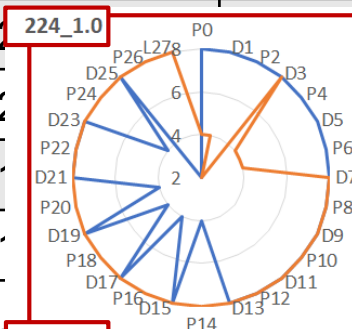
# Experimental Results on MobilenetV1

Iso-memory MobilenetV1 models with 2MB FLASH and 512kB RAM.

Integer-only

Model	Mparams	Full-Prec	Mix-PC	Mix-PL
224_1.0	4.24	<b>70.9</b>	64.3	59.6
192_1.0	4.24	70.0	65.9	61.9
224_0.75	2.24	<b>68.0</b>	<b>67.0</b>	
192_0.75	2.24		67.2	64.8
224_0.5	1.24		63.5	63.1
192_0.5	1.24		62.0	59.5

Higher drop due to more aggressive cuts



Quantization-aware

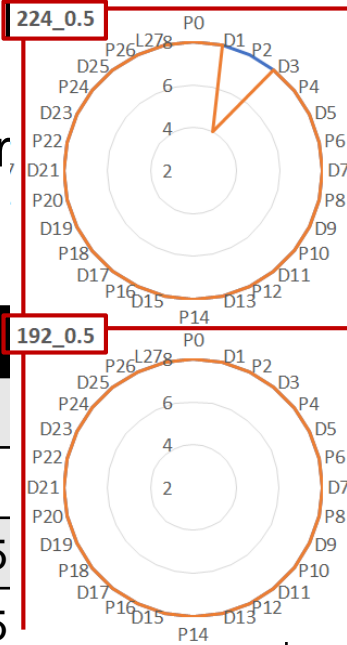
- Init w/ pre-train
- 8H on 4 NVIDIA
- ADAM, lr=1e-4
- Frozen batch
- Asymmetric qu
- (min/max) or F
- Asymmetric ac

Open source: <https://github.com/mrusci/training-mixed-precision-quantized-networks>



# Experimental Results on MobilenetV1

Iso-mer



V1 models with 2MB FLASH and 512kB RAM.

Integer-only

Model	I-Prec	Mix-PC	Mix-PL
224_1.0	9	64.3	59.6
192_1.0	0	65.9	61.9
224_0.75	4	<b>68.0</b>	<b>67.0</b>
192_0.75	2	67.2	64.8
<b>224_0.5</b>	1.34	63.3	63.1
<b>192_0.5</b>	1.34	61.7	59.5

Higher drop due to more aggressive cuts

Lossless, ~8 bit fits the memory constraints

Quantization-aware Fine-Tuning recipe:

- Init w/ pre-trained params
- 8H on 4 NVIDIA Tesla P100
- ADAM, lr=1e-4 (5e-5 @5ep, 1e-5 at 8 eph)
- Frozen batch norm stats after 1 eph
- Asymmetric quant on weights, either PC (min/max) or PL (PACT)
- Asymmetric activation (PACT)

Open source: <https://github.com/mrusci/training-mixed-precision-quantized-networks>



# Experimental Results on MobilenetV1

Iso-memory MobilenetV1 models with 2MB FLASH and 512kB RAM.

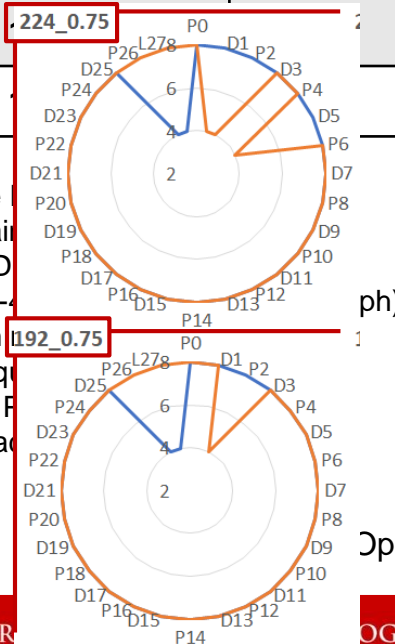
Integer-only

Model	Mparams	Full-Prec	Mix-PC	Mix-PL
224_1.0	4.24	70.9	64.3	59.6
192_1.0	4.24	70.0	65.9	61.9
224_0.75	2.59	68.4	68.0	67.0
192_0.75	2.59	67.2	67.2	64.8
224_0.5	1.76	62.0	63.5	63.1
192_0.5	1.76	62.0	62.0	59.5

Higher drop due to more aggressive cuts

Nearly lossless, few but 'significant' cuts ☺

Lossless, ~8 bit fits the memory constraints



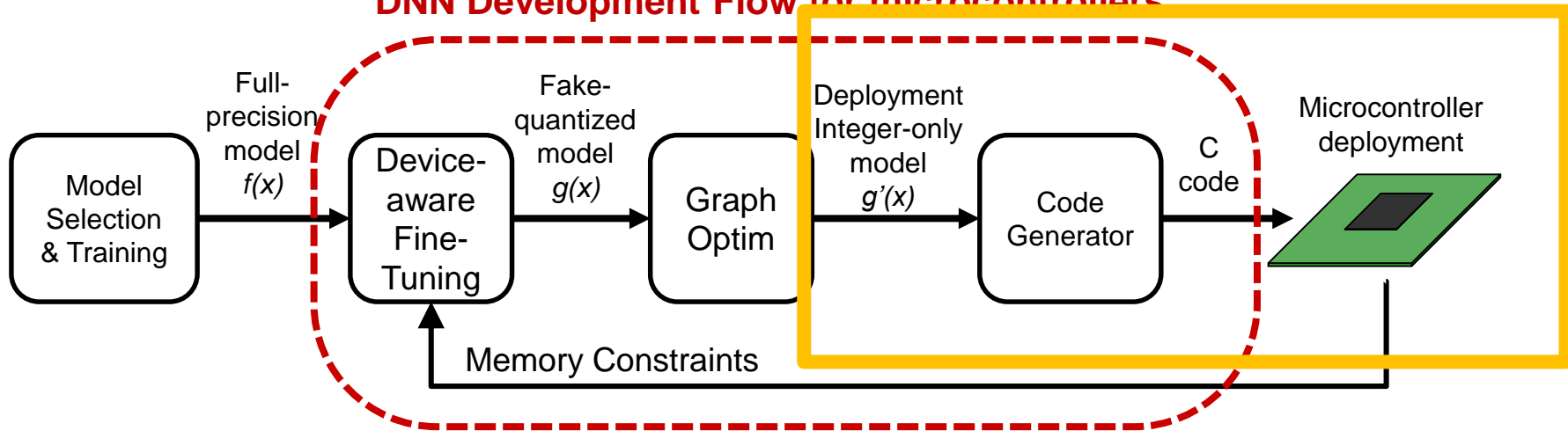
Quantization-aware

- Init w/ pre-train
- 8H on 4 NVIDIA
- ADAM, lr=1e-4
- Frozen batch norm
- Asymmetric quantization (min/max) or F
- Asymmetric activation

Overall, an integer-only network running on MCU with -2.9% accuracy drop wrt to the most precise model

Open source: <https://github.com/mrusci/training-mixed-precision-quantized-networks>

## DNN Development Flow for microcontrollers



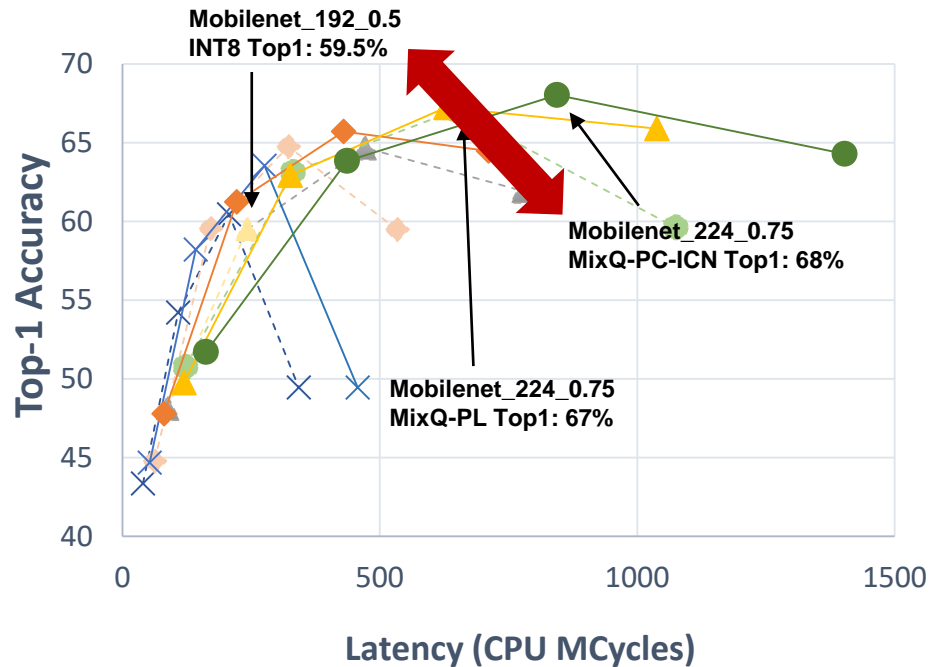
Deployments on MCUs

# LATENCY-ACCURACY TRADE-OFF ON A STM32H7 MCU



# Latency-Accuracy Trade Off

Experiments runs on a STM32H743 (400MHz clk)



- x-- 128-MixQ-PL
- ▲-- 192-MixQ-PL
- x— 128-MixQ-PC-ICN
- ▲— 192-MixQ-PC-ICN
- o- 160-MixQ-PL
- 224-MixQ-PL
- o- 160-MixQ-PC-ICN
- 224-MixQ-PC-ICN

- The implementation is based on the sw lib for mixed-precision inference (based on Cmsis-NN):
  - ❑ Cmix-NN: <https://github.com/EEESlab/CMix-NN>
  - ❑ UINT2-4 software emulated
  - ❑ MAC 2x16 bits
- PC on the pareto
- But PC slower than PL by 20-30%

$$\begin{aligned}
 \Phi &= \sum (X_q - Z_x) \cdot (W_q - Z_w) \\
 &= \sum X_{im2col} \cdot (W_q - Z_w) && \text{PC} \\
 &= \sum X_{im2col} \cdot W_q - \sum X_{im2col} \cdot Z_w && \text{PL}
 \end{aligned}$$

Overall +8% with respect to best 8-bit integer-only MobilenetV1 fitting the device (Jacob et al. 2018)



# Wrap-up

- We proposed an **end-to-end methodology** to train and deploy ‘complex’ DL models on **tiny MCUs**.
  - **sub-byte** uniform quantization
  - **mixed-precision** settings
  - a **memory-driven** rule-based method for determine the quantization policy
  - integer-only transformation with **ICN** activation layers
  - mixed precision **software** library for MCU
- Deployment of a 68% Imagenet MobilenetV1 into a MCU with 2MB FLASH and 512 kB RAM.